Math 1B Midterm 3 Non-Volume Review

- [1] Find the area of the region between $y = 4 x^2$ and $y = x^2 2x$ on [0, 4].
- [2] Find the area under the curve $y = \cos^{-1} x$.
- [3] A solid of revolution has volume $\int_{0}^{x} 2\pi (y+1)(1-\cos y) dy$. Sketch the region and the axis of revolution. Do not use the *x*- nor *y*-axes as boundaries nor the axis of revolution.
- [4] A solid of revolution has volume $\int_{1}^{4} \pi ((3+x)^2 (3-\sqrt{x})^2) dx$. Sketch the region and the axis of revolution.

Do not use the x- nor y-axes as boundaries nor the axis of revolution.

[5] Find the average value of
$$f(x) = \frac{\sin x}{1 + 4\cos^2 x}$$
 on $\left\lfloor \frac{\pi}{6}, \frac{\pi}{3} \right\rfloor$.

[6] If the average value of f on [-5, 6] is 7 and the average value of f on [2, 6] is -1, find $\int_{-5}^{2} f(x) dx$.

[7] Find the value of *c* guaranteed by the Mean Value Theorem for Integrals for $f(x) = \sqrt{64 - (x - 2)^2}$ on [-6, 2].

[8] Find the length of the curve
$$y = \frac{1}{8}x^4 + \frac{1}{4x^2}$$
 on [1, 2].

[9] Find the length of the curve
$$y = \int_{2}^{x} \sqrt{t^2 - 2t} dt$$
 on [2, 5].

[10] Find the area of the surface created by revolving the arc of $f(x) = \sqrt[3]{x}$ on [0, 8] about the y-axis.

[11] Find the area of the surface created by revolving the arc of $f(x) = \frac{x^4 + 3}{6x}$ on [1, 2] about the x-axis.

[12] A continuous random variable X with mean value 5.4 has probability density function $f(x) = \begin{cases} kx^n, & 0 \le x \le 9\\ 0, & x < 0 & or & x > 9 \end{cases}$

for some constants k and n.

- [a] Find k and n.
- [b] Find c such that the probability that X is less than c or greater than c are the same. (This is called the median value of X.)